



Quantum Machine Learning for HEP Detector Simulations

GRID 2021

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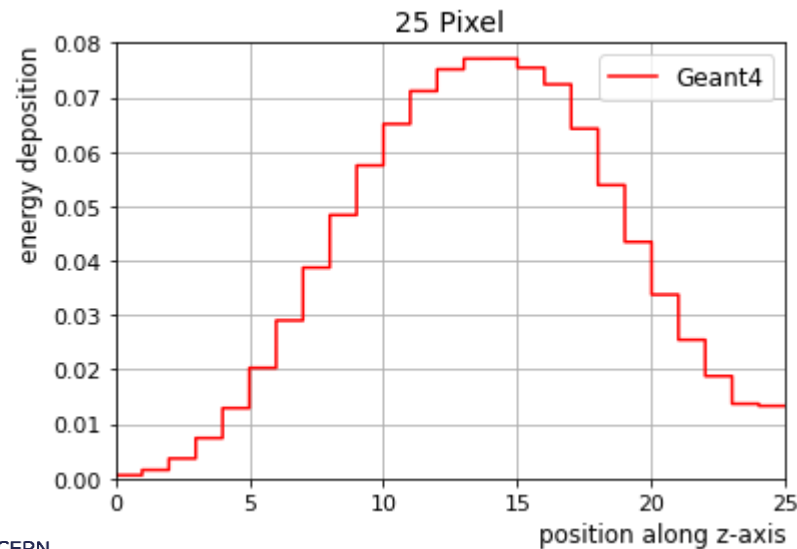
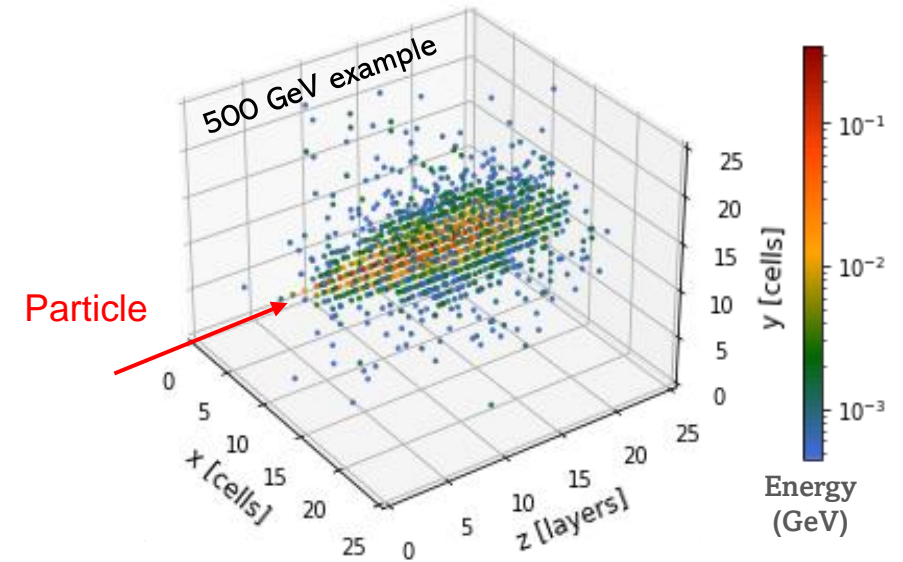
Future Simulations

Replace Calorimeter Monte Carlo Simulations

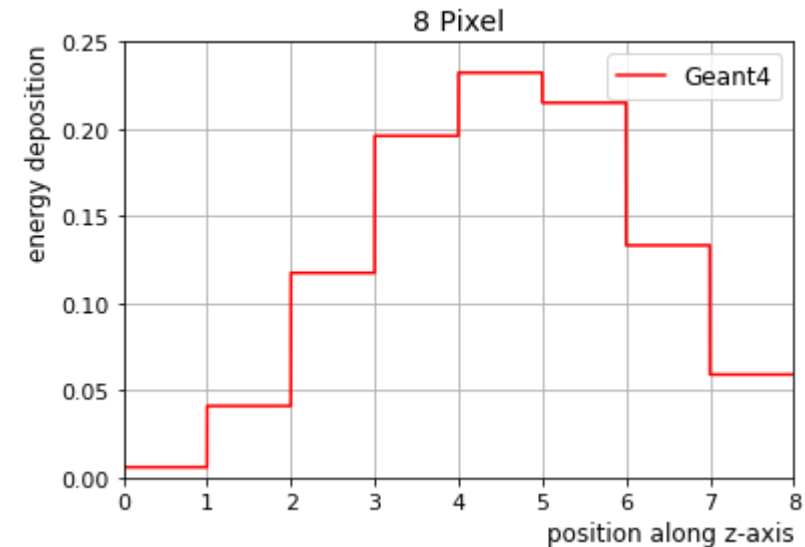
- Previously: **Deep Learning**
 - → Developed a Deep Learning approach for calorimeter simulations which requires fewer computing resources compared to Geant4
 - DL GAN presentation (up to 160 000x speed up)
 - On 06.07.2021 at 14:45 in GRID “Big data Analytics and Machine” block
- Now: **Explore potential of quantum computing**
 - Make use of quantum properties (entanglement, superposition)
 - Hope to solve problems faster and / or more accurately
 - “Quantum Advantage” not yet reached → only initial investigations
 - Understanding advantages and challenges
 - Using simplified models

Training Data

- 3D particle shower images
- Average the image over z-axis \rightarrow 1D image
- Down sample to only 8 pixel
- Average all of input energies \rightarrow Only one distribution



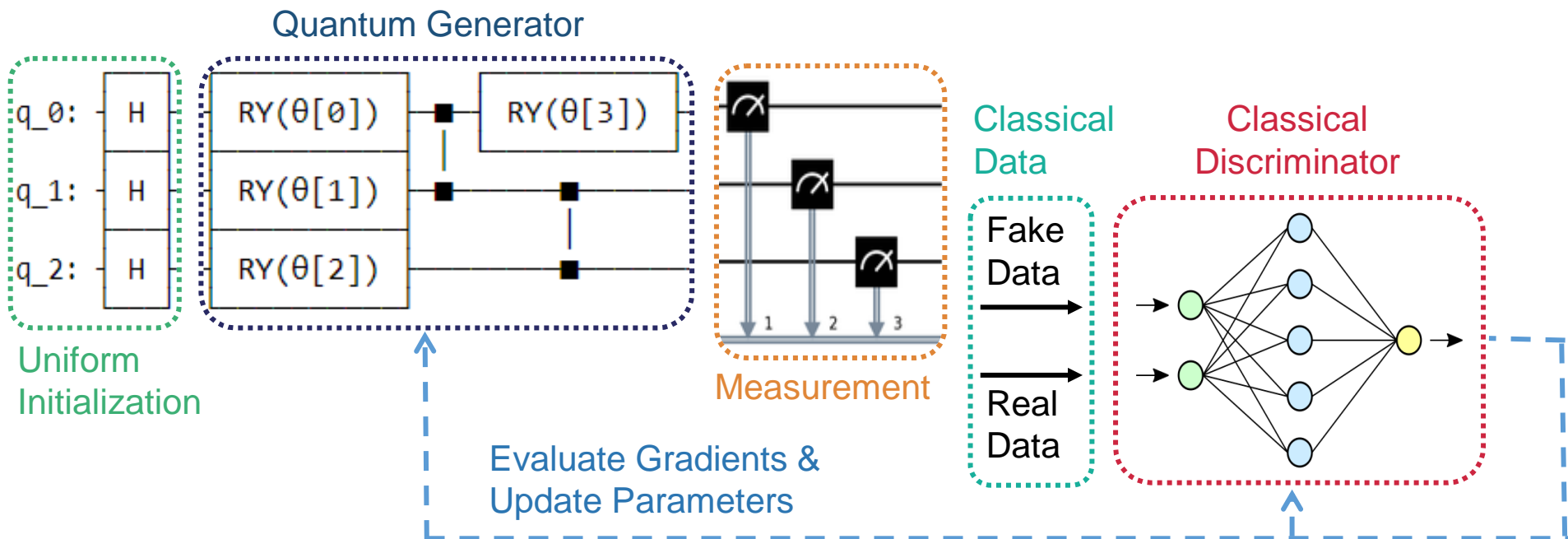
down sampling



Hybrid qGAN

Quantum Generative Adversarial Networks

- Hybrid quantum – classical ansatz



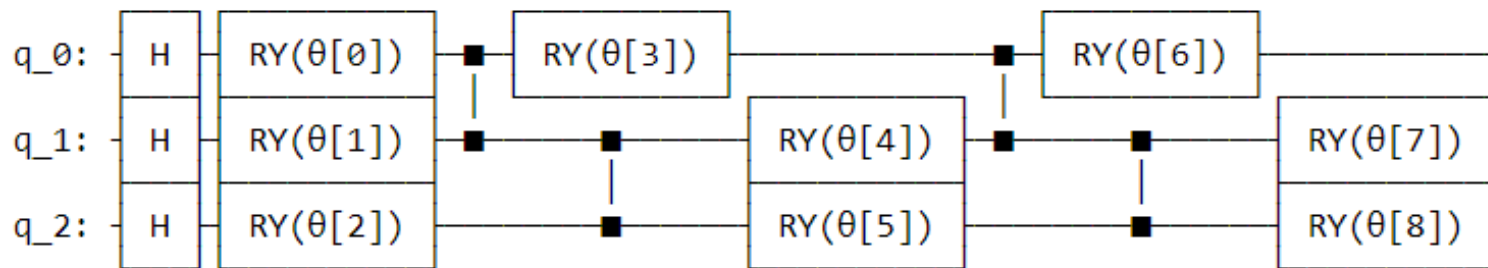


1D Quantum GAN

1D Quantum Generator Circuit

- Only 1D 8-pixel images
 - 3 qubits ($2^3 = 8$) in quantum generator circuit
 - 8 quantum states: $|000\rangle, |001\rangle, |010\rangle, |011\rangle, |100\rangle, |101\rangle, |110\rangle, |111\rangle$
- Modified a Qiskit qGAN model developed by IBM

Quantum Generator Circuit:



Gates:

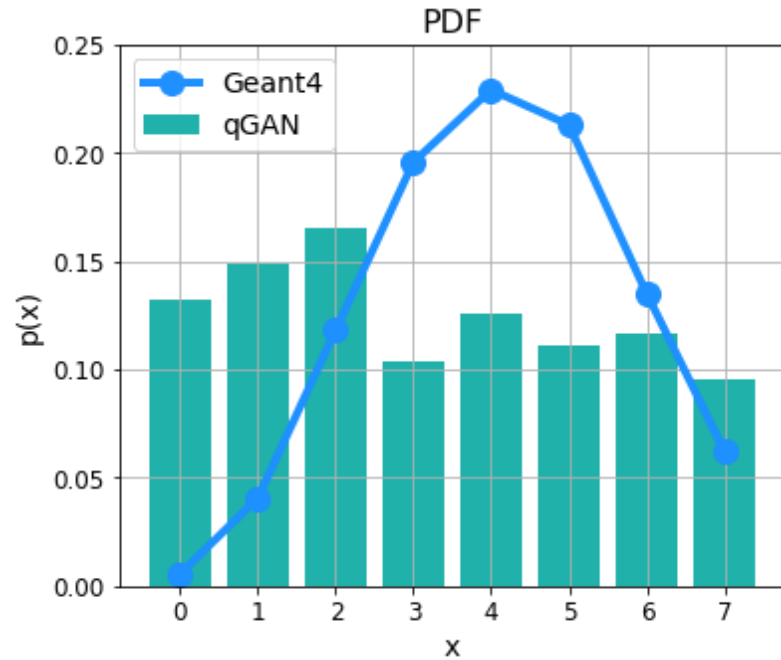
$$\boxed{H} = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$R_y(\theta) = \begin{pmatrix} \cos\left(\frac{\theta}{2}\right) & -\sin\left(\frac{\theta}{2}\right) \\ \sin\left(\frac{\theta}{2}\right) & \cos\left(\frac{\theta}{2}\right) \end{pmatrix}$$

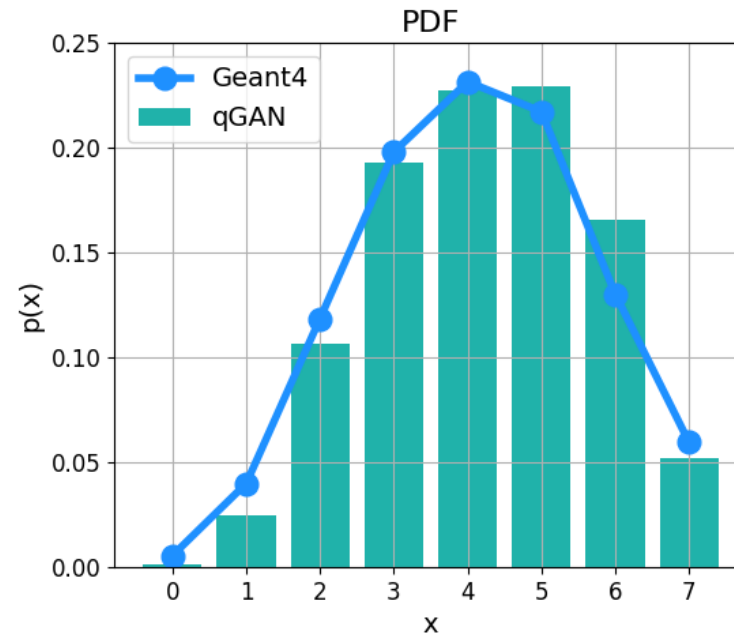
$$\begin{array}{c} \text{---} \\ | \\ \text{---} \end{array} \text{ or } \begin{array}{c} \text{---} \\ | \\ \boxed{Z} \\ | \\ \text{---} \end{array} = CZ = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

1D Quantum Simulator

Without Noise



Uniform Initialization



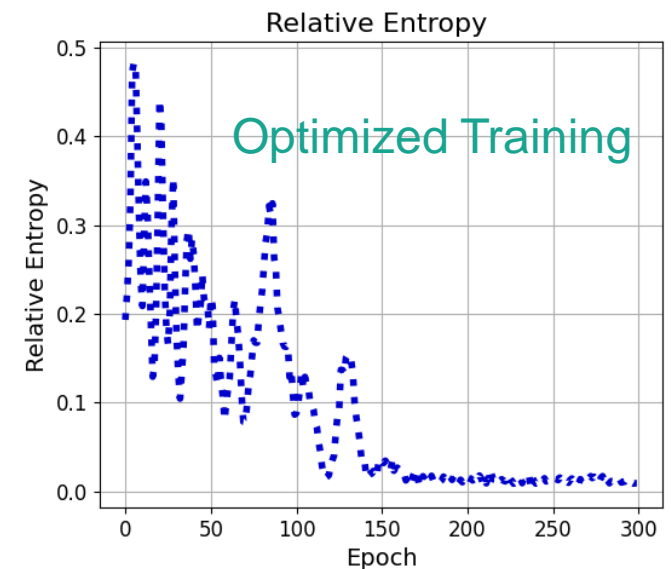
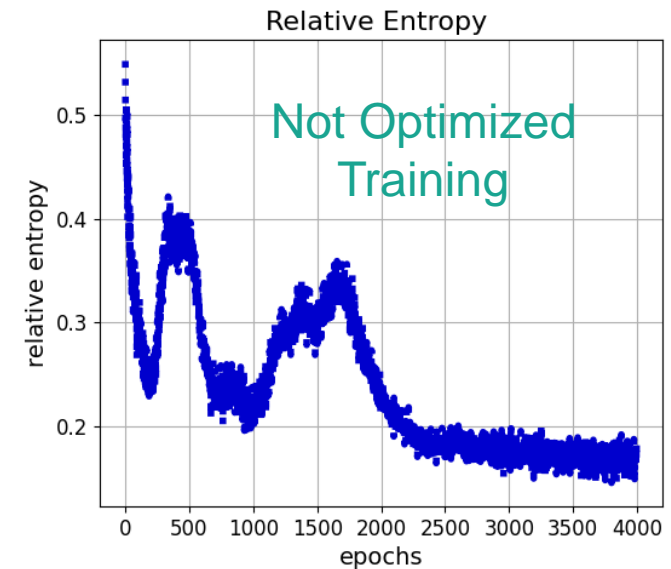
Trained Model

→ Good results

1D qGAN

Optimize Training

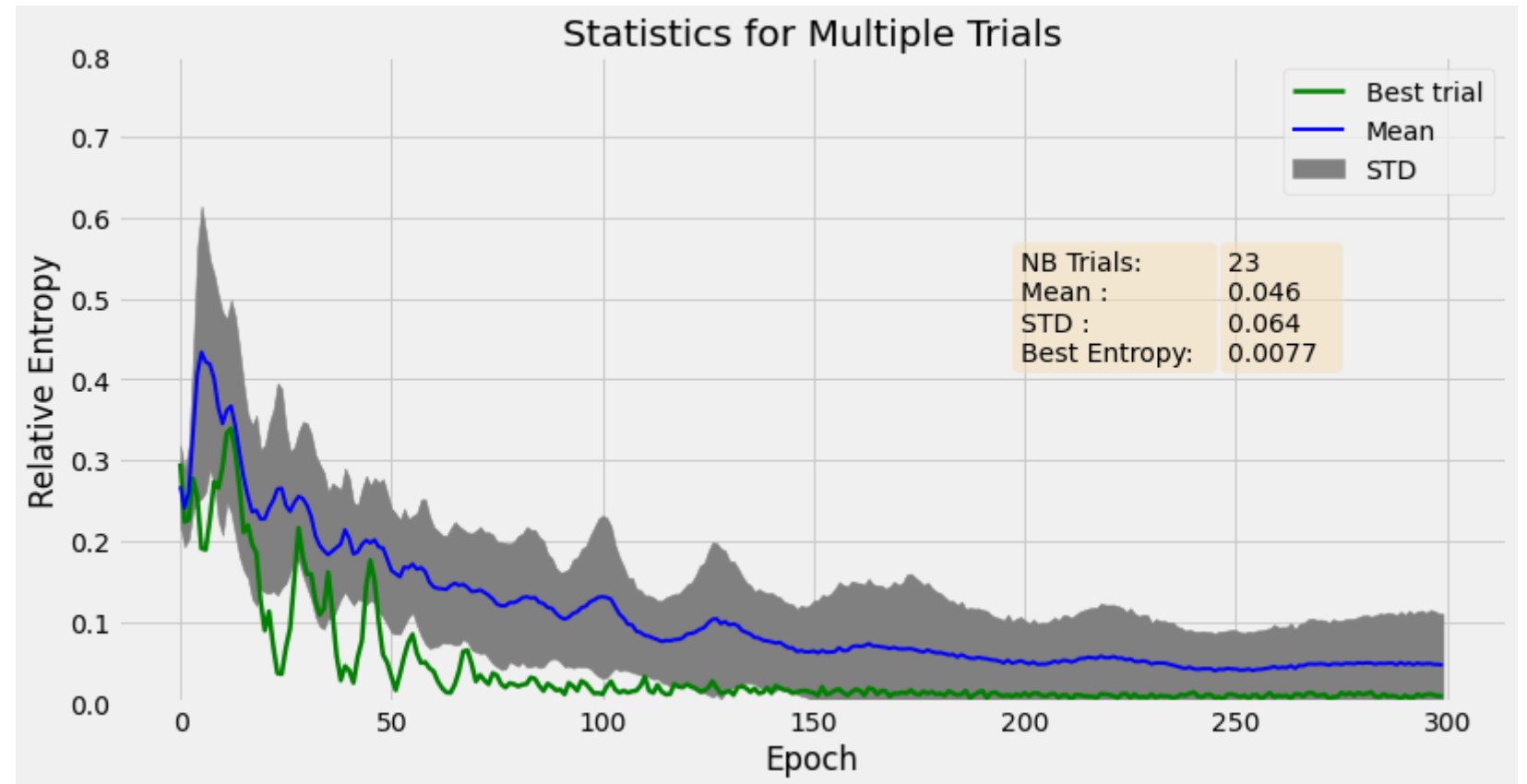
- Training time ~ 1 day for 3000 epochs
 - → speeding training up
- Hyperparameter optimizations:
 - Higher learning rate
 - Implement exponential learning rate decay
 - Different generator and discriminator learning rate
 - Train discriminator more often than generator
- Results:
 - **10x speed up** in training time
→ Only ~300 epochs instead of > 3000



1D qGAN Robustness

- Run 23 trials with same hyperparameters

→ Stable training
→ On average good accuracy

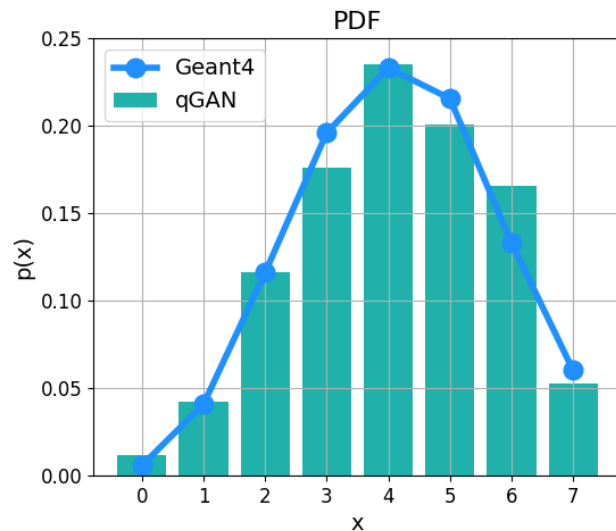


1D qGAN with Noise

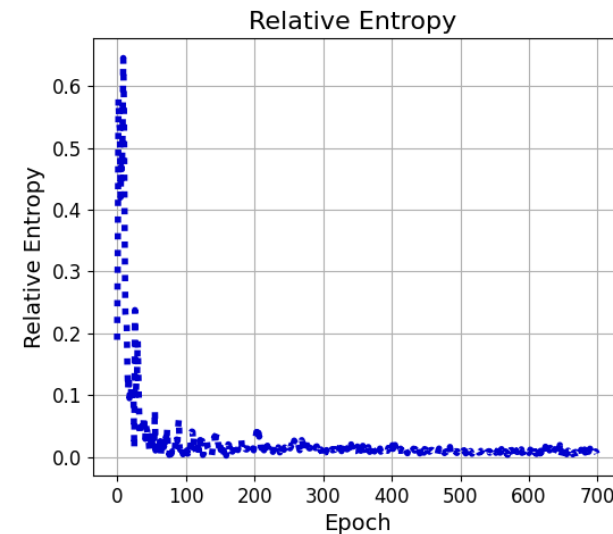
Readout Noise Only

- We applied readout noise to the qubit measurements
 - Noise model from IBMq belem quantum computer

Qubit Number	0	1	2
Readout Error	3.6%	4.7%	9.6%



→ No decrease in accuracy

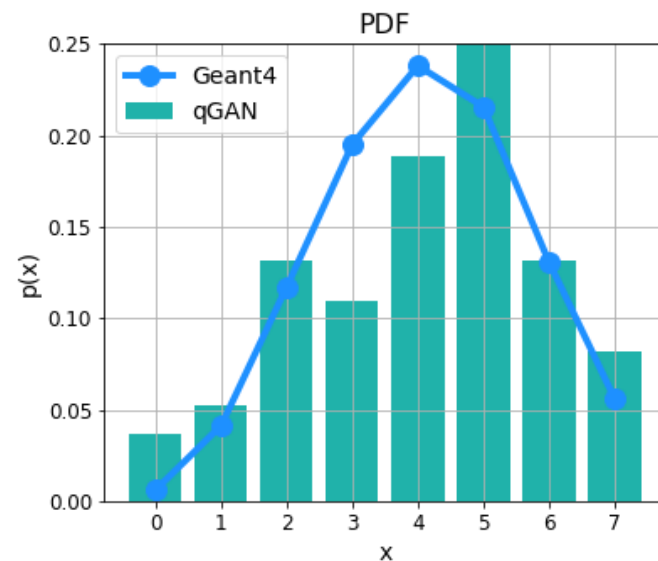


→ Fast convergence

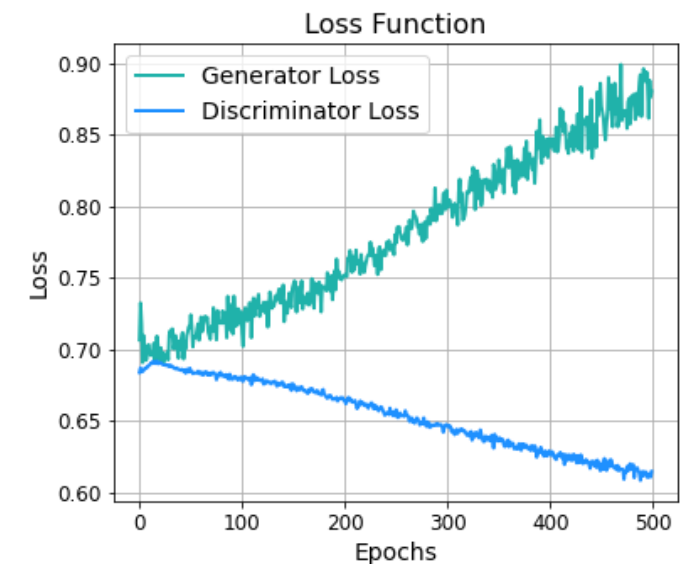
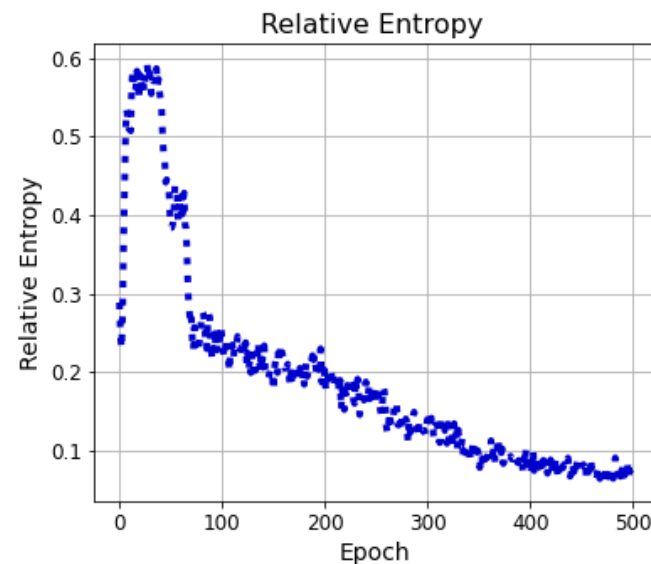
1D qGAN with Noise

Full Noise Model

- We applied noise to the qubit gates (readout noise + gate level noise)
 - Noise model from IBMq belem quantum computer
 - Average gate level noise: 4.32%



→ Lower accuracy



→ Non-converging losses



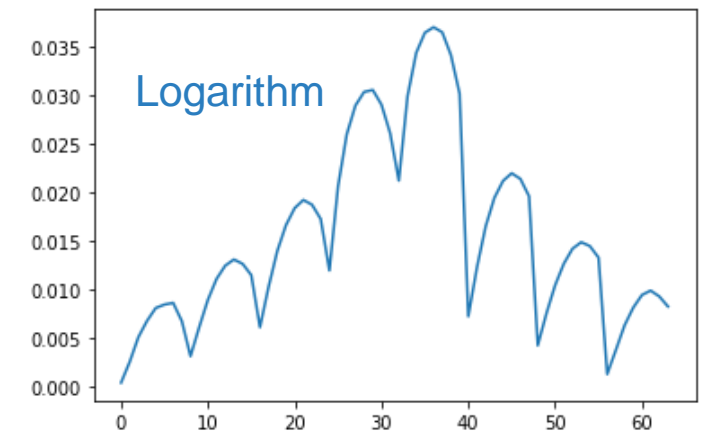
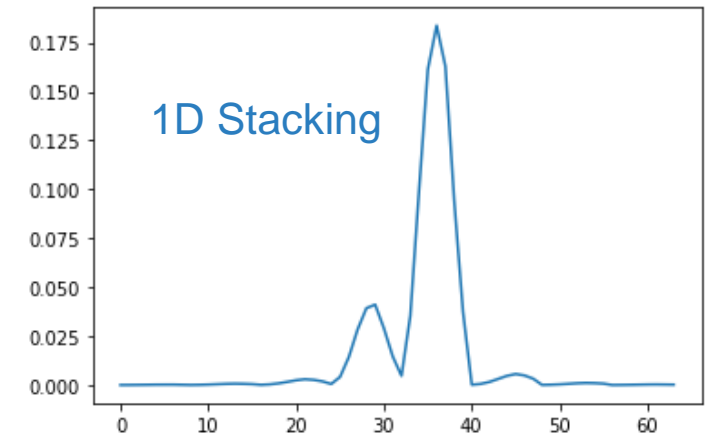
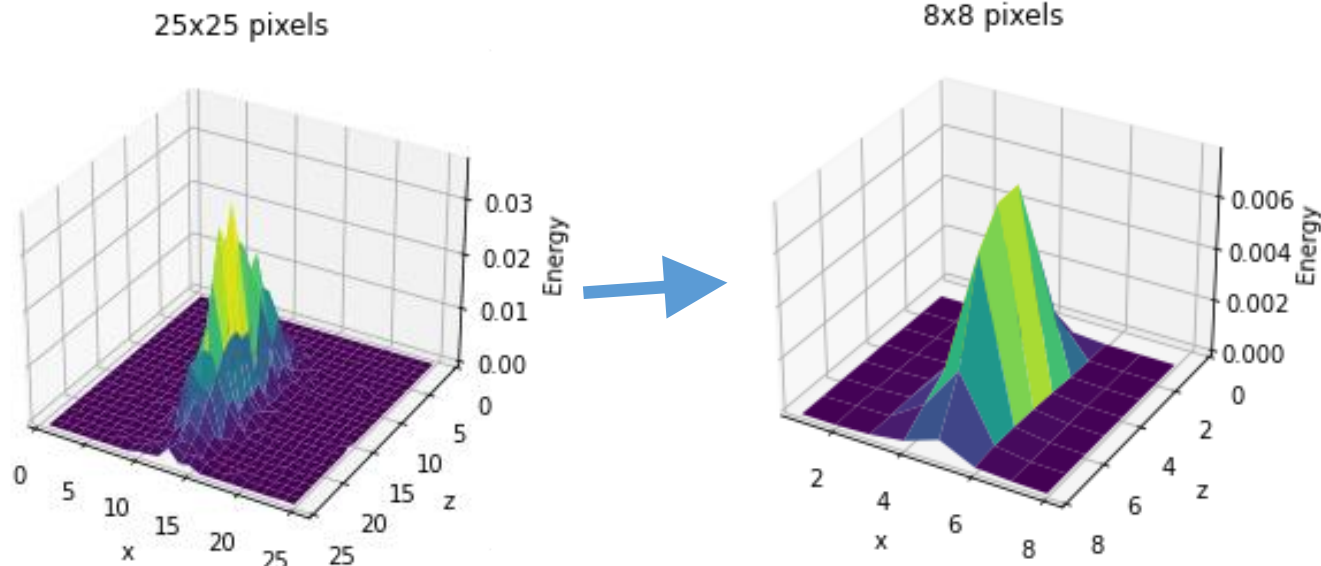
2D Quantum GAN

2D qGAN

2D Data Representation

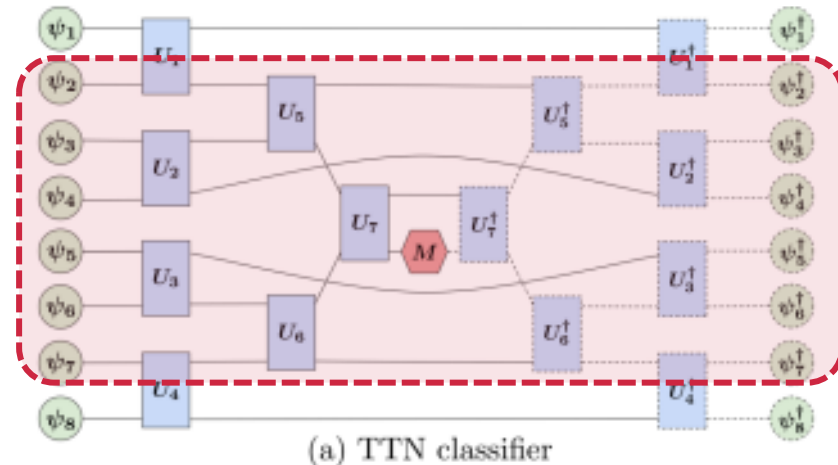
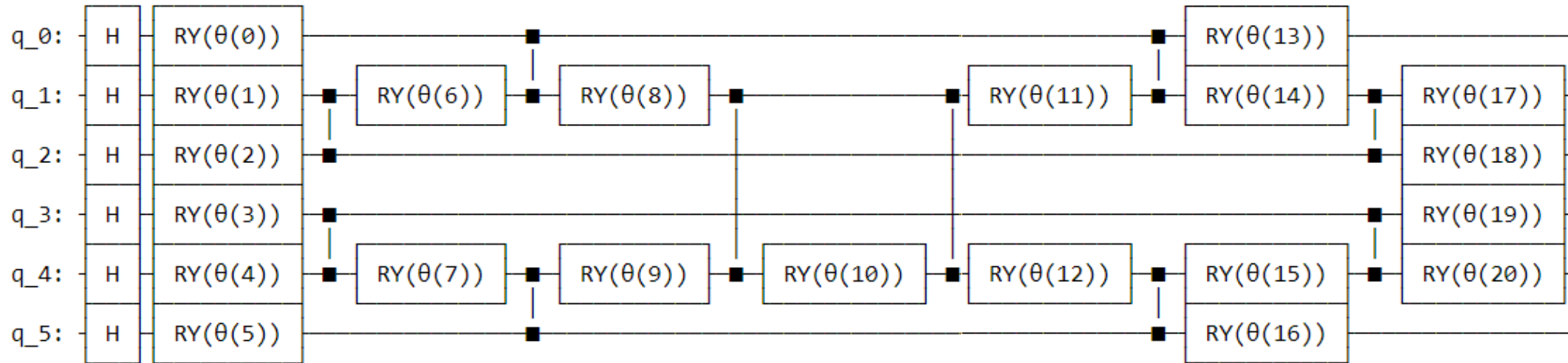
2D: $8 \times 8 = 64 \text{ pixels} = 2^6 \rightarrow 6 \text{ qubits}$

1. Down sample
2. 1D stacking
3. Apply logarithm



2D Quantum Generator Circuit

Tree Tensor Network Architecture



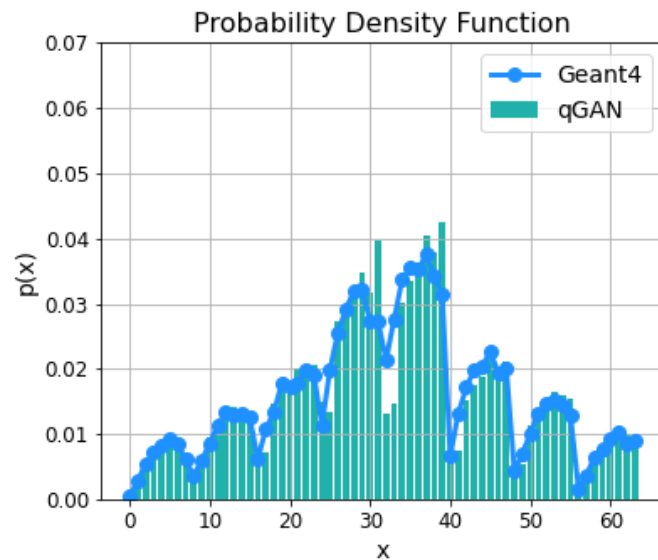
Only 6 qubits

Grant, E., Benedetti, M., Cao, S. *et al.* Hierarchical quantum classifiers. *npj Quantum Inf* **4**, 65 (2018). <https://doi.org/10.1038/s41534-018-0116-9>

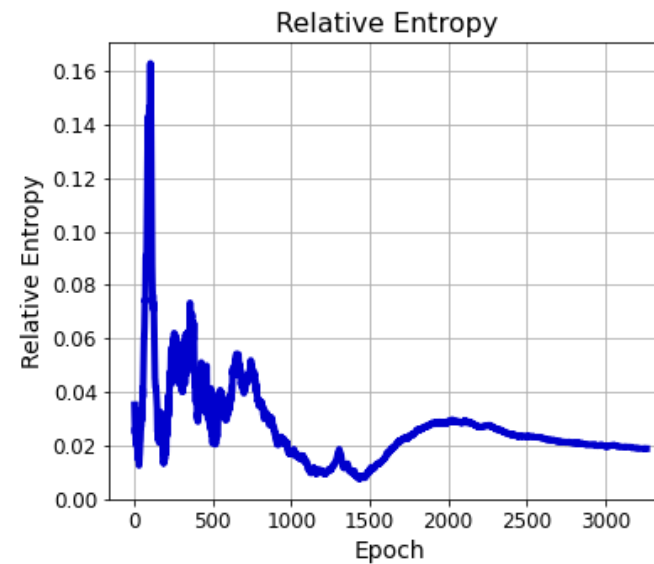
2D qGAN

Best Results

- Run on quantum simulator without noise



Trained Model



qGAN Future Work

- 2D qGAN:
 - Improve training convergence
 - Rare that training converges
 - Decrease training time: recently ~5 days
 - Hyperparameter optimization
- 1D qGAN:
 - More tests with the full noise model
 - Test error mitigation techniques
 - Conditional qGAN



QUESTIONS?

Quantum Machine Learning for HEP Detectors Simulations

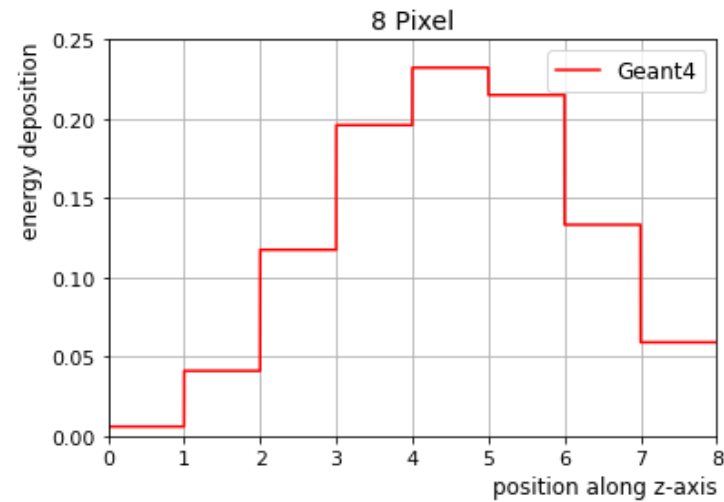
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Back Up Slides

Backup: Amplitude Encoding



Amplitude Encoding (2 qubit example)

State:	$ 00\rangle$	$ 01\rangle$	$ 10\rangle$	$ 11\rangle$
Pixel Nb:	0	1	2	3